

**PITTSBURG STATE UNIVERSITY**  
**DEPARTMENT OF MATHEMATICS**

Colloquium

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**Paradoxical Decompositions of Subsets in Euclidian Spaces.  
Can we make two balls out of one ball? Can we make a square  
out of a circle?**

Abstract

We say that two subsets  $A$  and  $B$  of the Euclidean space  $\mathbb{R}^n$  are equidecomposable if there is a partition of  $A$  into finitely many pieces  $\{A_i : i < k\}$  which can be rearranged by some isometries  $\{g_i : i < k\}$  to form a partition  $\{g_i(A_i) : i < k\}$  of  $B$  (roughly speaking, we can “cut”  $A$  into finitely many pieces and reassemble them to form  $B$ ). We will discuss some famous examples of equidecomposable sets, like Banach-Tarski paradox, that is, equidecomposability of the unit ball  $B$  in to two copies of  $B$  in 3-dimensional space. Another spectacular example is Laczkovich’s solution of the Tarski’s circle-squaring problem.

Tuesday, November 21, 2000  
2:00 p.m.  
Yates 215

Students are encouraged to attend.  
There will be cookies and conversation afterwards in Yates 210