

Name:.....

11+10+12+10+6+12+9+10+4+5+4+7

Show your work!

1 Fill in the following blanks:

- (a) Probabilities are real numbers between ____ and ____, inclusive.
- (b) $P(\text{Sample Space}) =$ _____.
- (c) $P(\text{Empty Set}) =$ _____.
- (d) If two events A and B are mutually exclusive then $P(A \cup B) =$ _____.
- (e) In general $P(A \cup B) =$ _____.
- (f) $P(A') =$ _____.
- (g) Greek letter μ is the symbol for _____.
- (h) Greek letter σ is the symbol for _____.
- (i) Symbol for the empty set is _____.
- (j) $(A')' =$ _____.

2 Consider the experiment of rolling a balanced six-sided die. Sample space $S = \{1, 2, 3, 4, 5, 6\}$. Let $A = \{1, 3, 5\}$ and $B = \{3, 6\}$. Find

- (a) $A \cup B$;
- (b) $A \cup B'$;
- (c) $A \cap B'$;
- (d) $A' \cap B'$;
- (g) $A' \cup B'$.

3 Given the mutually exclusive events Y and Z , for which $P(Y) = 0.28$, and $P(Z) = 0.47$, find

(a) $P(Y')$;

(b) $P(Y \cap Z)$;

(c) $P(Y \cup Z)$;

(d) $P(Y' \cap Z')$;

(e) $P(Y' \cup Z')$;

(f) $P(Y' \cap Z)$.

4 Let a random variable X have a binomial distribution with $n = 8$ and $p = 0.3$. Find the following.

(a) $P(X = 2)$

(b) $P(X \text{ is at least } 5)$

(c) $P(X \text{ is less than } 2)$

(d) $P(X \text{ is more than } 4)$

(e) $P(X \text{ is at most } 2)$

5 A civil service examination is designed so that 80% of all high school graduates can pass. Find the probabilities that among 14 high school graduates

(a) at least 12 will pass the test;

(b) at most 10 will pass the test.

6 Find the **mean**, **variance** and the **standard deviation** of the following distribution.

X	0	1	2
$f(x)$	0.4	0.2	0.4

- 7 The following table gives the exact breakdown of 400 inmates in a prison according to their sentences and the status as first or multiple offenders.

	<i>A</i>	<i>A'</i>	Total
<i>B</i>	120	40	
<i>B'</i>	80	160	
Total			

Let $A = \{\text{Sentences less than five years}\}$ and $B = \{\text{First offenders}\}$. If an inmate is randomly selected, find the following probabilities.

- (a) $P(B) = P(\text{Being a first time offender})$.
- (b) $P(A \cap B) = P(\text{First time offender whose sentence is less than five years})$.
- (c) $P(A | B) = P(\text{Having a sentence of less than five years given that the inmate is a first time offender})$.

Part 2

Name:.....

- 8 Find the following probabilities using the standard normal distribution. Draw a normal probability graph for each part and shade the area of interest.

(10 points)

(a) $P(Z \leq 0)$.

(b) $P(Z \leq 1.58)$.

(c) $P(Z \leq -1.58)$.

(d) $P(-1.58 \leq Z \leq -1.08)$.

(e) $P(-1.58 \leq Z \leq 1.08)$.

- 9 Find the points Z^* such that:

(4 points)

(a) $P(0 \leq Z \leq Z^*) = 0.4949$:

(b) $P(Z < Z^*) = 0.0051$.

Draw a normal probability graph for each part and shade the area of interest and mark the point of interest.

10 Let the random variable X have a normal distribution with the mean 30 and the standard deviation 4. Find the following: (5 points)
Draw graphs for parts (d) and (e).

(a) Z score when $X = 35$.

(b) Z score when $X = 22$.

(c) Z score when $X = 38$.

(d) $P(35 \leq X \leq 38)$.

(e) $P(22 \leq X \leq 38)$.

11 If z_a denotes the value of z for which the area under the standard normal curve to its right is equal to a , find (4 points)
Draw graphs.

(a) $Z_{0.005}$;

(b) $Z_{0.05}$.

12 The lengths of the sardines received by a cannery have a mean of 4.75 inches and a standard deviation of 0.25 inches. If the distribution of these lengths can be approximated closely with a normal distribution, what percentage of all these sardines are (7 points)

(a) longer than 4.25 inches;

(b) from 4.50 to 5.5 inches long? **Draw graphs.**