

Elementary Statistics

Test 2

Fall 2009

Name:.....

10+3+3+5+3+3+10+9+12+12+10+8+12

1 Let  $S = \{1, 2, 3, 4, 5, 6\}$ ,  $A = \{1, 2, 3\}$ , and  $B = \{2, 5\}$ . Find the following sets.

(a)  $A \cap B$

(b)  $A \cup B$

(c)  $A \cap B'$

(d)  $A' \cap B'$

(e)  $A \cup B'$

2 If  $P(A) = 0.65$  then find  $P(A')$ .

3 What is the value of  $P(S)$ ?

4 If  $A \cap B = \phi$ ,  $P(A) = 0.48$ , and  $P(B) = 0.3$ , then find  $P(A \cup B)$ .

5 What are the odds for the occurrence if its probability is 0.65?

6 Convert 3 to 7 odds to probability.

7 If  $P(A) = 0.42$ ,  $P(B) = 0.27$ , and  $P(A \cap B) = 0.17$ , then find the following:

(a)  $P(A \cup B)$

(b)  $P(A' \cup B')$

(c)  $P(A \cap B')$

(d)  $P(A' \cap B')$

(e)  $P(A \cup B')$

8 The data below, in thousands, represent the age of persons receiving Medicaid and their poverty level. (Source: U.S. Census Bureau)

	Under 18 years (A)	18 years and over (A')
Below Poverty Level (B)	8,550	6,834
Above Poverty Level (B')	5,884	7,440

(a) Among those receive Medicaid, what percent is below the poverty level?  
Or find  $P(B)$ .

(b) Among those receive Medicaid, what percent is above the poverty level and under 18 years of age?  
Or find  $P(A \cap B')$ .

(c) Among those receive Medicaid, if a randomly selected person is under 18 years of age, what is the probability that he or she is below poverty level?  
That is find  $P(B|A)$ .

9 Let  $X$  have a Binomial distribution with  $n = 6$  and  $p = 0.4$ . Find the following:

(a)  $P(X = 2)$

(b)  $P(X < 2)$

(c)  $P(X \leq 2)$

(d)  $P(X > 2)$

(e)  $P(X \geq 2)$

10 Consider the following distribution.

$X$	1	2	3
$P(X)$	0.7	0.2	0.1

Find

(a) Mean

(b) Variance

(c) Standard deviation

11 Find the following probabilities using the standard normal distribution. Draw a normal probability graph for each part and shade the area of interest.

(a)  $P(Z \leq 0)$ .

(b)  $P(Z \leq 1.58)$ .

(c)  $P(Z \leq -1.08)$ .

(d)  $P(-1.58 \leq Z \leq -1.08)$ .

(e)  $P(-1.58 \leq Z \leq 1.08)$ .

12 If  $z_\alpha$  denotes the value of  $Z$  for which the area under the standard normal curve to its right is equal to  $\alpha$ , find

(a)  $z_{0.0228}$ ;

(b)  $z_{0.0250}$ ;

**Also draw a normal probability graph for each part and shade the area of interest and mark the point of interest.**

13 Let the random variable  $X$  have a normal distribution with the mean 50 and the standard deviation 4. Find the following:

**Also draw graphs for parts (d) and (e).**

(a)  $Z$  score when  $X = 55$ .

(b)  $Z$  score when  $X = 42$ .

(c)  $Z$  score when  $X = 58$ .

(d)  $P(55 \leq X \leq 58)$ .

(e)  $P(42 \leq X \leq 58)$ .