Elementary Statistics

TEST 2

Fall 2010

Name:....

10+2+2+5+2+2+10+9+10+12+10+8+11+4+3=100

- Let $S = \{1, 2, 3, 4, 5, 6\}$, $A = \{2, 3, 5\}$, and $B = \{4, 5\}$. Find the following sets.
 - (a) $A \cap B$
 - (b) $A \cup B$
 - (c) $A \cap B'$
 - (d) $A' \cap B'$
 - (e) $A \cup B'$
- 2 If P(A) = 0.05 then find P(A').
- 3 What is the value of $P(\phi)$?
- 4 If $A \cap B = \phi$, P(A) = 0.27, and P(B) = 0.35, then find $P(A \cup B)$.

- What are the odds for the occurrence if its probability is 0.35?
- 6 Convert 13 to 7 odds to probability.

- 7 If P(A) = 0.47, P(B) = 0.37, and $P(A \cap B) = 0.27$, then find the following:
 - (a) $P(A \cup B)$
 - (b) $P(A' \cup B')$
 - (c) $P(A \cap B')$
 - (d) $P(A' \cap B')$
 - (e) $P(A \cup B')$
- The data below, in thousands, represent the age of persons receiving Medicaid and their poverty level. (Source: U.S. Census Bureau)

	Under 18 years (A)	18 years and over (A')
Below Poverty Level (B)	8,550	6,834
Above Poverty Level (B')	5,884	7,440

- (a) Among those receive Midicaid, what percent is below the poverty level? Or find P(B).
- (b) Among those receive Midicaid, what percent is above the poverty level and under 18 years of age? Or find $P(A \cap B')$.
- (c) Among those receive Midicaid, if a randomly selected person is under 18 years of age, what is the probability that he or she is below poverty level? That is find P(B|A).

9 Let X have a Binomial distribution with n = 6 and p = 0.7. Find the following:

(a)
$$P(X = 2) = \text{Probability of } X \text{ is equal to } 2$$

(b)
$$P(X < 2) = \text{Probability of X is less than 2}$$

(c)
$$P(X \le 2) = \text{Probability of } X \text{ is at most } 2$$

(d)
$$P(X > 2) = \text{Probability of X is more than 2}$$

(e)
$$P(X \ge 2)$$
 = Probability of X is at least 2

10 Consider the following distribution.

X	1	2	3
P(X)	0.3	0.3	0.4

Find

- (a) Mean
- (b) Variance

(c) Standard deviation

11	Find the following probabilities using the standard normal distribution.	Also draw a
	normal probability graph for each part and shade the area of interest.	

(a)
$$P(Z \le 0)$$
.

(b)
$$P(Z \le 1.58)$$
.

(c)
$$P(Z \le -1.08)$$
.

(d)
$$P(-1.58 \le Z \le -1.08)$$
.

(e)
$$P(-1.58 \le Z \le 1.08)$$
.

If
$$z_{\alpha}$$
 denotes the value of Z for which the area under the standard normal curve to its right is equal to α , find

(a)
$$z_{0.0668}$$
;

(b)
$$z_{0.05}$$
;

- Let the random variable *X* have a normal distribution with the mean 50 and the standard deviation 5. Find the following: **Draw graphs for parts (d) and (e).**
 - (a) Z score when X = 57.
 - (b) Z score when X = 40.
 - (c) Z score when X = 52.
 - (d) $P(52 \le X \le 57)$.

- (e) $P(40 \le X \le 57)$.
- What are the four basic rules of probability?

Find the third quartile of the standard normal distribution.